

1. *Single-ended list*.
2. Abstract Data Types (ADTs: stack using *single-ended list* and queue using *double-ended list*).
3. Specialized list (*doubly linked list*).

1. Single-ended list

The single-ended list is a structure that characterizes quickly inserting and deleting a data. From exercise no. 3 we know data structure such as an array and a sorted array. Both structures have some disadvantages. In the case of an unsorted arrays, the search is slow, while in sorted arrays slow is inserting new items. It is also time-consuming for deleting an item in both types of arrays.

In the single-ended list, data is inside the object **Link**. Since there are usually many similar objects (**links**) in the list (list), it is reasonable to create a separate class for them. Each object of type Link contains (as a class field) pointer (**pNex**) to the next object of type Link.

Example 1 (C++; *single-ended list* = (*singly*) linked list) First approach to data structure: linked list.

[linkList.cpp]

```
//linkList.cpp
//demonstrates linked list
#include <iostream>
using namespace std;

class Link
{
public:
    int iData;           //data item
    double dData;        //data item
    Link* pNext;         //ptr to next link in list

    Link(int id, double dd) : //constructor
        iData(id), dData(dd), pNext(NULL)
    { }

    void displayLink()      //display ourself {22, 2.99}
    {
        cout << "{" << iData << ", " << dData << "}" << endl;
    }
}; //end class Link
//-----
class LinkList
{
private:
    Link* pFirst;         //ptr to first link on list

public:
    LinkList() : pFirst(NULL) //constructor
    { }                    //(no links on list yet)
```

```

bool isEmpty()                                //true if list is empty
{ return pFirst==NULL; }

//insert at start of list
void insertFirst(int id, double dd)
{
    Link* pNewLink = new Link(id, dd);        //make new link
    pNewLink->pNext = pFirst;                  //newLink-->old first
    pFirst = pNewLink;                        //first-->newLink
}

Link* getFirst()                              //return first link
{ return pFirst; }

void removeFirst()                            //delete first link
{                                              //(assumes list not empty)
    Link* pTemp = pFirst;                    //save first
    pFirst = pFirst->pNext;                  //unlink it: first-->old next
    delete pTemp;                          //delete old first
}

void displayList()
{
    cout << "List (first-->last): ";
    Link* pCurrent = pFirst;                //start at beginning of list
    while(pCurrent != NULL)                  //until end of list,
    {
        pCurrent->displayLink();             //print data
        pCurrent = pCurrent->pNext;          //move to next link
    }
    cout << endl;
}

}; //end class LinkList
//-----
int main()
{
    LinkList theList;                       //make new list

    theList.insertFirst(22, 2.99);           //insert four items
    theList.insertFirst(44, 4.99);
    theList.insertFirst(66, 6.99);
    theList.insertFirst(88, 8.99);

    theList.displayList();                   //display list

    while( !theList.isEmpty() )              //until it's empty,
    {
        Link* pTemp = theList.getFirst();    //get first link
                                                //display its key
        cout << "Removing link with key " << pTemp->iData << endl;
        theList.removeFirst();               //remove it
    }
    theList.displayList();                   //display empty list
    return 0;
} //end main()

```

Finding and removing the specific objects (Links)

The next example will include two additional methods. These methods can be applied to:

- search list item that contains a variable with a specific value,
- deleting the item of the list containing a variable with the specified value.

Example 2 (C++; (singly) linked list) Second version of data structure: linked list.

[linkList2.cpp]

```
//linkList2.cpp
//demonstrates linked list
#include <iostream>
using namespace std;

class Link
{
public:
    int iData;           //data item (key)
    double dData;        //data item
    Link* pNext;         //next link in list

    Link(int id, double dd) : //constructor
        iData(id), dData(dd), pNext(NULL)
    { }

    void displayLink()        //display ourself: {22, 2.99}
    {
        cout << "{" << iData << ", " << dData << "} ";
    }
}; //end class Link
//-----
class LinkList
{
private:
    Link* pFirst;         //ptr to first link on list

public:
    LinkList() : pFirst(NULL) //constructor
    { }                     //(no links on list yet)

    ~LinkList()           //destructor (deletes links)
    {
        Link* pCurrent = pFirst; //start at beginning of list
        while(pCurrent != NULL) //until end of list,
        {
            Link* pOldCur = pCurrent; //save current link
            pCurrent = pCurrent->pNext; //move to next link
            delete pOldCur;           //delete old current
        }
    }

    void insertFirst(int id, double dd)
    {
        //make new link
        Link* pNewLink = new Link(id, dd);
        pNewLink->pNext = pFirst; //it points to old first link
        pFirst = pNewLink;       //now first points to this
    }
}
```

```

Link* find(int key)                //find link with given key
{                                  //(assumes non-empty list)
    Link* pCurrent = pFirst;      //start at 'first'
    while(pCurrent->iData != key)  //while no match,
    {
        if(pCurrent->pNext == NULL) //if end of list,
            return NULL;           //didn't find it
        else                       //not end of list,
            pCurrent = pCurrent->pNext; //go to next link
    }
    return pCurrent;              //found it
}

bool remove(int key)              //remove link with given key
{                                  //(assumes non-empty list)
    Link* pCurrent = pFirst;      //search for link
    Link* pPrevious = pFirst;
    while(pCurrent->iData != key)
    {
        if(pCurrent->pNext == NULL)
            return false;         //didn't find it
        else
        {
            pPrevious = pCurrent; //go to next link
            pCurrent = pCurrent->pNext;
        }
    }
    //found it
    if(pCurrent == pFirst)        //if first link,
        pFirst = pFirst->pNext;  //change first
    else                          //otherwise,
        pPrevious->pNext = pCurrent->pNext; //bypass it
    delete pCurrent;             //delete link
    return true;                 //successful removal
}

void displayList()               //display the list
{
    cout << "List (first-->last): ";
    Link* pCurrent = pFirst;      //start at beginning of list
    while(pCurrent != NULL)       //until end of list,
    {
        pCurrent->displayLink();  //print data
        pCurrent = pCurrent->pNext; //move to next link
    }
    cout << endl;
}
}; //end class LinkList
//-----
int main()
{
    LinkList theList;             //make list

    theList.insertFirst(22, 2.99); //insert 4 items
    theList.insertFirst(44, 4.99);
    theList.insertFirst(66, 6.99);
    theList.insertFirst(88, 8.99);

    theList.displayList();        //display list

    int findKey = 44;             //find item
    Link* pFind = theList.find(findKey);

```

```

    if( pFind != NULL)
        cout << "Found link with key " << pFind->iData << endl;
    else
        cout << "Can't find link" << endl;

    int remKey = 66; //remove item
    bool remOK = theList.remove(remKey);
    if( remOK )
        cout << "Removed link with key " << remKey << endl;
    else
        cout << "Can't remove link" << endl;

    theList.displayList(); //display list
    return 0;
} //end main()

```

Member function **find()**

The **find()** works like `displayList()` from program `linkList.cpp`. Initially `pCurrent` pointer is set to point to the same object as `pFirst`. Every time element in the list we need to set `pCurrent` on `pCurrent -> pNext`. Each list item is checked if storage search value. If the searched value is found, it returns a pointer to the list item. If the end of the list is reach without finding the item with storage value `NULL` pointer is returned.

2. Abstract Data Types

What are Abstract Data Types (ADTS)? Roughly speaking, it is a way of looking at the data structure: focus on what needs to be done (with the data structure), ignoring the method of operation of data structures.

ADT is the concept of data structures separated from implementation. As examples of abstract data types can be stacks and queues. Separating data structures from their implementation will be shown also by stacks and queues, but now we'll use a linked list not as previously arrays.

Implementation of stack based on a linked list

Implementation **push()** and **pop()**

On the classes 04-05 to create a stack, we used class `vector` (for data storage). Operations on the stack have been done using function `push()` and `pop()` as operations on vectors, ie. The operation of adding (pushing) to the stack

```
stackVect[++top] = data;
```

and operation removing (popping) from the stack

```
data = stackVect[top--];
```

Data storage on stack may also be implemented by using the linked list. In this case, the operations `pop()` and `push()` are implemented by operations such as

```
theList.insertFirst(data)
```

and

```
data = theList.deleteFirst()
```

User of the stack class calls the `push()` and `pop()` to add and to delete an element, without knowledge (or the need for knowledge) about whether the stack is implemented as an array or as a linked list.

Example 3 (C++; (singly) linked list) Example of implementation of the stack (class `LinkStack`) using a class `LinkList` instead of an array.

[linkStack.cpp]

```
//linkStack.cpp
//demonstrates a stack implemented as a list
#include <iostream>
using namespace std;

class Link
{
public:
    double dData;           //data item
    Link* pNext;            //next link in list

    Link(double dd) : dData(dd), pNext(NULL)
    { }                    //constructor

    void displayLink()      //display ourself
    { cout << dData << " "; }
}; //end class Link
//-----
class LinkList
{
private:
    Link* pFirst;           //ptr to first item on list

public:
    LinkList() : pFirst(NULL) //constructor
    { }

    ~LinkList()              //destructor (deletes links)
    {
        Link* pCurrent = pFirst; //start at beginning of list
        while(pCurrent != NULL) //until end of list,
        {
            Link* pOldCur = pCurrent; //save current link
            pCurrent = pCurrent->pNext; //move to next link
            delete pOldCur;           //delete old current
        }
    }

    bool isEmpty()           //true if list is empty
    { return (pFirst==NULL); }

    void insertFirst(double dd) //insert at start of list
    { //make new link
        Link* pNewLink = new Link(dd);
        pNewLink->pNext = pFirst; //newLink --> old first
        pFirst = pNewLink;       //first --> newLink
    }

    double deleteFirst()     //delete first item
    { }
```

```

    {
        Link* pTemp = pFirst;           //(assumes list not empty)
        pFirst = pFirst->pNext;          //save old first link
        double key = pTemp->dData;        //remove it: first-->old next
        delete pTemp;                   //remember data
        return key;                     //delete old first link
    }                                  //return deleted link's data

void displayList()                     //display all links
{
    Link* pCurrent = pFirst;           //start at beginning of list
    while(pCurrent != NULL)            //until end of list,
    {
        pCurrent->displayLink(); //print data
        pCurrent = pCurrent->pNext; //move to next link
    }
    cout << endl;
}

}; //end class LinkList
//-----
class LinkStack
{
private:
    LinkList* pList;                   //pointer to linked list
public:
    LinkStack()                        //constructor
    { pList = new LinkList; }          //make a linked list

    ~LinkStack()                       //destructor
    { delete pList; }                  //delete the linked list

    void push(double j)                //put item on top of stack
    { pList->insertFirst(j); }

    double pop()                       //take item from top of stack
    { return pList->deleteFirst(); }

    bool isEmpty()                     //true if stack is empty
    { return ( pList->isEmpty() ); }

    void displayStack()
    {
        cout << "Stack (top-->bottom): ";
        pList->displayList();
    }
}; //end class LinkStack
//-----
int main()
{
    LinkStack theStack;                //make stack

    theStack.push(20);                  //push items
    theStack.push(40);

    theStack.displayStack();            //display stack (40, 20)

    theStack.push(60);                  //push items
    theStack.push(80);

    theStack.displayStack();            //display (80, 60, 40, 20,)
}

```

```

theStack.pop();           //pop items (80, 60)
theStack.pop();

theStack.displayStack();  //display stack (40, 20)
return 0;
} //end main()

```

Relation between classes

Function `main()` is associated only with the class `LinkStack`. `LinkStack` class in turn is only associated with the class `LinkList`. Between the `main()` and class `LinkList` there is no direct communication.

Implementation of the stack with a linked list instead of arrays shows how interface can be disconnected (visible/available to the user class) from implementation of (hidden) stack.

Double-ended lists

The implementation of the queue will be done using double-ended list. Double-ended list is similar to the usual (singly) linked list (single-ended list) but now object list has a reference to the first `pFirst` and last `pLast` item of the list. Reference to the last item in the list allow us to attach easily a new item at the end of it as in the case of attaching an element to the beginning of the list (of course, it is possible to attach the element to the end of single-ended list going through all the elements of the list but it is more difficult and less efficient). Easy access to the first and last element of the the list is appropriate in situations where the standard single-ended list is not effective. An example here is the implementation of the queue.

Example 4 (C++) Implementation of double-ended list.

[firstLastList.cpp]

```

//firstLastList.cpp
//demonstrates list with first and last references
#include <iostream>
using namespace std;

class Link
{
public:
    double dData;           //data item
    Link* pNext;            //ptr to next link in list

    Link(double d) : dData(d), pNext(NULL) //constructor
    { }

    void displayLink()      //display this link
    { cout << dData << " "; }
}; //end class Link
//-----
class FirstLastList
{
private:

```

```

Link* pFirst;                //ptr to first link
Link* pLast;                 //ptr to last link

public:
FirstLastList() : pFirst(NULL), pLast(NULL)    //constructor
{ }

~FirstLastList()                //destructor
{                               // (deletes all links)
    Link* pCurrent = pFirst;    //start at beginning
    while(pCurrent != NULL)    //until end of list,
    {
        Link* pTemp = pCurrent; //remember current
        pCurrent = pCurrent->pNext; //move to next link
        delete pTemp;           //delete old current
    }
}

bool isEmpty()                //true if no links
{ return pFirst==NULL; }

void insertFirst(double dd)    //insert at front of list
{
    Link* pNewLink = new Link(dd); //make new link
    if( isEmpty() )                //if empty list,
        pLast = pNewLink;         //newLink <-- last
    pNewLink->pNext = pFirst;       //newLink --> old first
    pFirst = pNewLink;            //first --> newLink
}

void insertLast(double dd)     //insert at end of list
{
    Link* pNewLink = new Link(dd); //make new link
    if( isEmpty() )                //if empty list,
        pFirst = pNewLink;         //first --> newLink
    else
        pLast->pNext = pNewLink;   //old last --> newLink
    pLast = pNewLink;             //newLink <-- last
}

void removeFirst()             //remove first link
{                               //(assumes non-empty list)
    Link* pTemp = pFirst;         //remember first link
    if(pFirst->pNext == NULL)      //if only one item
        pLast = NULL;            //NULL <-- last
    pFirst = pFirst->pNext;        //first --> old next
    delete pTemp;                //delete the link
}

void displayList()
{
    cout << "List (first-->last): ";
    Link* pCurrent = pFirst;      //start at beginning
    while(pCurrent != NULL)       //until end of list,
    {
        pCurrent->displayLink();   //print data
        pCurrent = pCurrent->pNext; //move to next link
    }
    cout << endl;
}
}; //end class FirstLastList

```

```
//-----
int main()
{
    FirstLastList theList;           //make a new list

    theList.insertFirst(22);          //insert at front
    theList.insertFirst(44);
    theList.insertFirst(66);

    theList.insertLast(11);           //insert at rear
    theList.insertLast(33);
    theList.insertLast(55);

    theList.displayList();            //display the list

    cout << "Deleting first two items" << endl;
    theList.removeFirst();             //remove first two items
    theList.removeFirst();

    theList.displayList();            //display again
    return 0;
} //end main()
```

Implementation of the queue using double-ended list

Example 5 (C++; double-ended list) Implementation of data structure: the queue (you can compare with the program Queue.cpp from classes No. 5 example 2).

[linkQueue.cpp]

```
//linkQueue.cpp
//demonstrates queue implemented as double-ended list
#include <iostream>
using namespace std;

class Link
{
public:
    double dData;           //data item
    Link* pNext;             //ptr to next link in list

    Link(double d) :dData(d), pNext(NULL) //constructor
    { }

    void displayLink()       //display this link
    { cout << dData << " "; }
}; //end class Link
//-----
class FirstLastList
{
private:
    Link* pFirst;           //ptr to first link
    Link* pLast;            //ptr to last link

public:
    FirstLastList() : pFirst(NULL), pLast(NULL) //constructor
    { }
}
```

```

~FirstLastList()                //destructor
{                                // (deletes all links)
    Link* pCurrent = pFirst;    //start at beginning
    while(pCurrent != NULL)     //until end of list,
    {
        Link* pTemp = pCurrent; //remember current
        pCurrent = pCurrent->pNext; //move to next link
        delete pTemp;           //delete old current
    }
}

bool isEmpty()                  //true if no links
{ return pFirst==NULL; }

void insertLast(double dd)      //insert at end of list
{
    Link* pNewLink = new Link(dd); //make new link
    if( isEmpty() )               //if empty list,
        pFirst = pNewLink;       //first --> newLink
    else
        pLast->pNext = pNewLink;  //old last --> newLink
    pLast = pNewLink;            //newLink <-- last
}

double removeFirst()            //delete first link
{                                //(assumes non-empty list)
    Link* pTemp = pFirst;        //remember first link
    double temp = pFirst->dData;
    if(pFirst->pNext == NULL)     //if only one item
        pLast = NULL;           //null <-- last
    pFirst = pFirst->pNext;       //first --> old next
    delete pTemp;               //delete the link
    return temp;
}

void displayList()
{
    Link* pCurrent = pFirst;     //start at beginning
    while(pCurrent != NULL)      //until end of list,
    {
        pCurrent->displayLink();  //print data
        pCurrent = pCurrent->pNext; //move to next link
    }
    cout << endl;
}
}; //end class FirstLastList
//-----
class LinkQueue
{
private:
    FirstLastList theList;

public:
    bool isEmpty()                //true if queue is empty
    { return theList.isEmpty(); }

    void insert(double j)         //insert, rear of queue
    { theList.insertLast(j); }

    double remove()              //remove, front of queue

```

```

        { return theList.removeFirst(); }

    void displayQueue()
    {
        cout << "Queue (front-->rear): ";
        theList.displayList();
    }
}; //end class LinkQueue
//-----
int main()
{
    LinkQueue theQueue;           //make a queue

    theQueue.insert(20);           //insert items
    theQueue.insert(40);

    theQueue.displayQueue();       //display queue (20, 40)

    theQueue.insert(60);           //insert items
    theQueue.insert(80);

    theQueue.displayQueue();       //display queue (20, 40, 60, 80)

    cout << "Removing two items" << endl;
    theQueue.remove();             //remove items (20, 40)
    theQueue.remove();

    theQueue.displayQueue();       //display queue (60, 80)
    return 0;
} //end main()

```

3. Specialized list

Implementation of doubly linked list

Doubly linked list provides the ability to pass the list in both directions. In the doubly linked list each element of the list has two pointers (instead of one as in the singly linked list). The first pointer points to the next element (as in the usual list). The second pointer points to the preceding element.

The beginning of the declaration of the doubly linked list:

```

class Link
{
    public:
        double dData;           //data item
        Link* pNext;             //next link in list
        Link* pPrevious;         //previous link in list
};

```

Inserting an element to the front of the list

```

void insertFirst(double dd)           //insert at front of list
{
    Link* pNewLink = new Link(dd);    //make new link
    if( isEmpty() )                  //if empty list,
        pLast = pNewLink;           //newLink <-- last
    else
        pFirst->pPrevious = pNewLink; //newLink <-- old first
        pNewLink->pNext = pFirst;     //newLink --> old first
        pFirst = pNewLink;           //first --> newLink
}

```

Inserting an element to the list after element containing searched data

```

if(pCurrent==pLast)                  //if last link,
{
    pNewLink->pNext = NULL;           //newLink --> null
    pLast = pNewLink;               //newLink <-- last
}
else                                 //not last link,
{
    pNewLink->pNext = pCurrent->pNext; //newLink --> old next
    pCurrent->pNext->pPrevious = pNewLink; //newLink <-- old next
}
pNewLink->pPrevious = pCurrent; //old current <-- newLink
pCurrent->pNext = pNewLink;     //old current --> newLink

```

Example 6 (C++) Implementation of data structure of type: doubly linked list.

[doublyLinked.cpp]

```

//doublyLinked.cpp
//demonstrates doubly-linked list
#include <iostream>
using namespace std;

class Link
{
public:
    double dData;           //data item
    Link* pNext;            //next link in list
    Link* pPrevious;        //previous link in list

public:
    Link(double dd) :       //constructor
        dData(dd), pNext(NULL), pPrevious(NULL)
    { }

    void displayLink()      //display this link
    { cout << dData << " "; }
}; //end class Link
//-----
class DoublyLinkedList
{
private:
    Link* pFirst;           //pointer to first item
}

```

```

Link* pLast;                                //pointer to last item

public:
DoublyLinkedList() :                        //constructor
    pFirst(NULL), pLast(NULL)
{ }

~DoublyLinkedList()                          //destructor (deletes links)
{
    Link* pCurrent = pFirst;                //start at beginning of list
    while(pCurrent != NULL)                  //until end of list,
    {
        Link* pOldCur = pCurrent;          //save current link
        pCurrent = pCurrent->pNext;          //move to next link
        delete pOldCur;                     //delete old current
    }
}

bool isEmpty()                              //true if no links
{ return pFirst==NULL; }

void insertFirst(double dd)                  //insert at front of list
{
    Link* pNewLink = new Link(dd);           //make new link
    if( isEmpty() )                          //if empty list,
        pLast = pNewLink;                   //newLink <-- last
    else
        pFirst->pPrevious = pNewLink;         //newLink <-- old first
        pNewLink->pNext = pFirst;             //newLink --> old first
        pFirst = pNewLink;                   //first --> newLink
}

void insertLast(double dd)                   //insert at end of list
{
    Link* pNewLink = new Link(dd);           //make new link
    if( isEmpty() )                          //if empty list,
        pFirst = pNewLink;                   //first --> newLink
    else
    {
        pLast->pNext = pNewLink;              //old last --> newLink
        pNewLink->pPrevious = pLast;           //old last <-- newLink
    }
    pLast = pNewLink;                         //newLink <-- last
}

void removeFirst()                           //remove first link
{                                              //(assumes non-empty list)
    Link* pTemp = pFirst;
    if(pFirst->pNext == NULL)                 //if only one item
        pLast = NULL;                       //null <-- last
    else
        pFirst->pNext->pPrevious = NULL;       //null <-- old next
        pFirst = pFirst->pNext;               //first --> old next
        delete pTemp;                         //delete old first
}

void removeLast()                            //remove last link
{                                              //(assumes non-empty list)
    Link* pTemp = pLast;
    if(pFirst->pNext == NULL)                 //if only one item
        pFirst = NULL;                       //first --> null
}

```

```

        else
            pLast->pPrevious->pNext = NULL; //old previous --> null
            pLast = pLast->pPrevious;        //old previous <-- last
            delete pTemp;                    //delete old last
    }

    //insert dd just after key
bool insertAfter(double key, double dd)
{
    // (assumes non-empty list)
    Link* pCurrent = pFirst; //start at beginning
    while(pCurrent->dData != key) //until match is found,
    {
        pCurrent = pCurrent->pNext; //move to next link
        if(pCurrent == NULL)
            return false; //didn't find it
    }
    Link* pNewLink = new Link(dd); //make new link
    if(pCurrent==pLast) //if last link,
    {
        pNewLink->pNext = NULL; //newLink --> null
        pLast = pNewLink; //newLink <-- last
    }
    else //not last link,
    { //newLink --> old next
        pNewLink->pNext = pCurrent->pNext;
        //newLink <-- old next
        pCurrent->pNext->pPrevious = pNewLink;
    }
    pNewLink->pPrevious = pCurrent; //old current <-- newLink
    pCurrent->pNext = pNewLink; //old current --> newLink
    return true; //found it, did insertion
}

bool removeKey(double key) //remove item w/ given key
{
    // (assumes non-empty list)
    Link* pCurrent = pFirst; //start at beginning
    while(pCurrent->dData != key) //until match is found,
    {
        pCurrent = pCurrent->pNext; //move to next link
        if(pCurrent == NULL)
            return false; //didn't find it
    }
    if(pCurrent==pFirst) //found it; first item?
        pFirst = pCurrent->pNext; //first --> old next
    else //not first
        //old previous --> old next
        pCurrent->pPrevious->pNext = pCurrent->pNext;

    if(pCurrent==pLast) //last item?
        pLast = pCurrent->pPrevious; //old previous <-- last
    else //not last
        //old previous <-- old next
        pCurrent->pNext->pPrevious = pCurrent->pPrevious;
    delete pCurrent; //delete item
    return true; //successful deletion
}

void displayForward()
{
    cout << "List (first-->last): ";
    Link* pCurrent = pFirst; //start at beginning

```

```

        while(pCurrent != NULL)           //until end of list,
        {
            pCurrent->displayLink();       //display data
            pCurrent = pCurrent->pNext;     //move to next link
        }
        cout << endl;
    }

    void displayBackward()
    {
        cout << "List (last-->first): ";
        Link* pCurrent = pLast;           //start at end
        while(pCurrent != NULL)           //until start of list,
        {
            pCurrent->displayLink();       //display data
            pCurrent = pCurrent->pPrevious; //go to previous link
        }
        cout << endl;
    }
}; //end class DoublyLinkedList
//-----
int main()
{
    DoublyLinkedList theList;             //make a new list

    theList.insertFirst(22);              //insert at front
    theList.insertFirst(44);
    theList.insertFirst(66);

    theList.insertLast(11);               //insert at rear
    theList.insertLast(33);
    theList.insertLast(55);

    theList.displayForward();              //display list forward
    theList.displayBackward();            //display list backward

    cout << "Deleting first, last, and 11" << endl;
    theList.removeFirst();                 //remove first item
    theList.removeLast();                  //remove last item
    theList.removeKey(11);                 //remove item with key 11

    theList.displayForward();              //display list forward

    cout << "Inserting 77 after 22, and 88 after 33" << endl;
    theList.insertAfter(22, 77);           //insert 77 after 22
    theList.insertAfter(33, 88);           //insert 88 after 33

    theList.displayForward();              //display list forward
    return 0;
} //end main()

```

Based on:

Robert Lafore - "Teach Yourself Data Structures And Algorithms In 24 Hours"